

# Noise Analysis of CMOS Common-Source/Drain Active Balun

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## I. CIRCUIT OVERVIEW

Common-source/drain active balun circuit is composed of just single transistor M1 as shown in Fig. 1, designed in complementary metal-oxide semiconductor (CMOS) technology. This active balun circuit is considered as the simplest topology amongst other active balun configurations. The input signal is fed into the gate of the transistor, and normal operation results in an inverted output signal at RFout2 and a non-inverted signal at RFout1. Ideally, the two outputs would have the same amplitude with a phase shift or difference of 180°. Load resistors R1 and R2 determine the output voltages as well as the voltage gains of the two output signals with respect to the input signal.

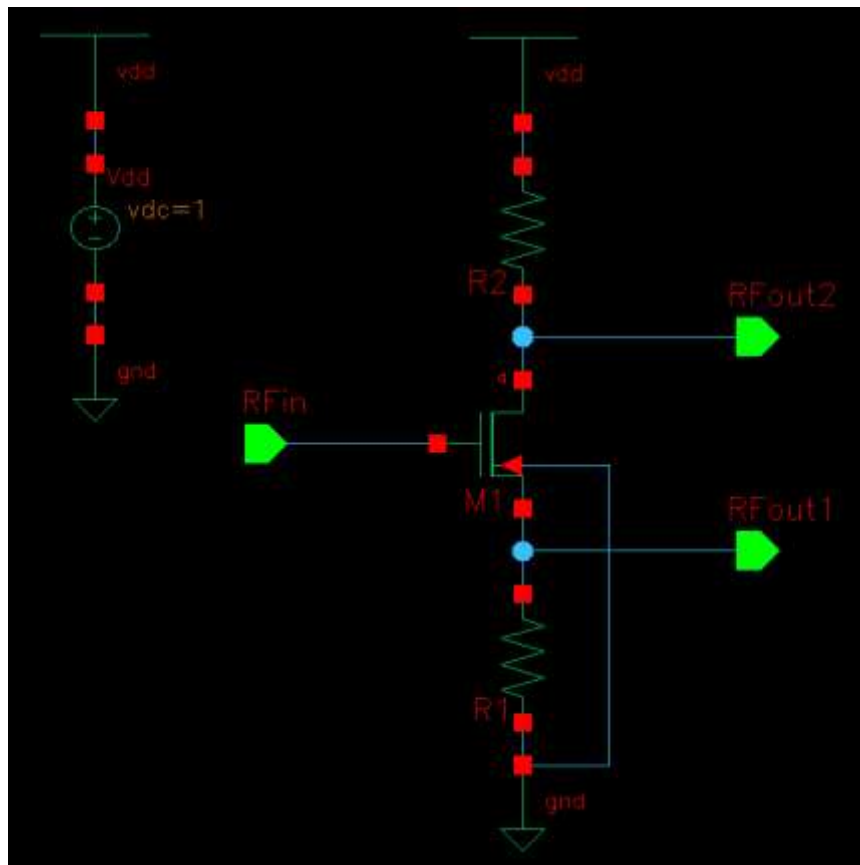


Fig. 1. Common-source/drain active balun schematic diagram.

Common-source topology exhibits a relatively high input impedance while providing voltage gain and requiring a minimal voltage headroom. Common-drain topology or source-follower, on the other hand, is occasionally employed as level shifters or buffers, impacting the overall frequency response. It also exhibits high input impedance. With the two topologies merged to function as an active balun, common-drain will dominate the response on the overall voltage gain or attenuation because of the feedback effect of load resistor R1 with respect to the input.

## II. NOISE ANALYSIS

Noise performance is an important design consideration since it determines the susceptibility of the active balun to unwanted signal or noise. Important design parameters such as signal-to-noise ratio (SNR), dynamic range (DR), and noise figure (NF) can be derived using noise analysis. Fig. 2 shows the circuit model with noise sources of common-source/drain active balun.

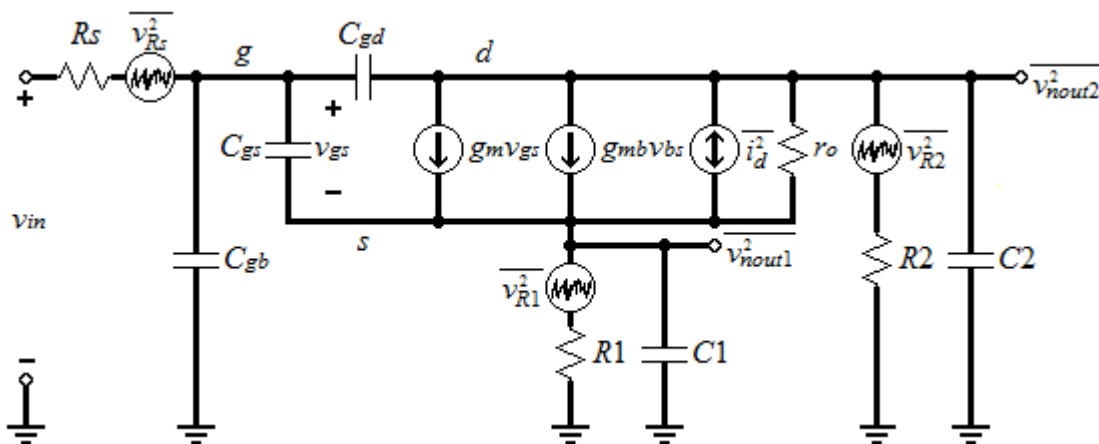


Fig. 2. Common-source/drain active balun circuit model with noise generator.

Since active balun supplies differential input signal into a differential circuit, noise calculation for each of the two output nodes is necessary. Succeeding discussions determine the output noise contributions of the active balun produced by the transistor itself and the output loads.

$$\overline{i_{n,out2}^2} = \overline{i_{d,th}^2} + \overline{i_{d,1/f}^2} + \overline{i_{R2}^2} + \frac{\overline{v_{Rs}^2} - \overline{v_{n,out2}^2}}{(1/sC_{gd})^2} \quad (1)$$

$$\overline{v_{n,out2}^2} = \left[ 4k_B T \gamma (g_m + g_{mb}) \Delta f + \frac{K_f I_D}{L^2 C_{ox} f_{co}} \Delta f + \frac{4k_B T}{R2} \Delta f + \frac{\overline{v_{Rs}^2} - \overline{v_{n,out2}^2}}{(1/sC_{gd})^2} \right] \left( R2 \parallel \frac{1}{sC2} \right)^2 \quad (2)$$

At higher frequency, thermal noise of transistor dominates, hence flicker noise could be neglected. Assuming source resistance to be zero, that is  $R_s = 0$ , and rearranging (2), output voltage noise of RFout2 could be simplified.

$$\overline{v_{n,out2}^2} = \frac{k_B T}{C2} \cdot \frac{1 + \gamma (g_m + g_{mb}) R2}{1 + \frac{1}{4} \left( \frac{C_{gd}}{C2} \right)^2} V_{rms}^2 \quad (3)$$

Assuming that  $C_{gd}$  is significantly smaller than the output load capacitance  $C2$ , (3) would be simplified as

$$\overline{v_{n,out2}^2} = \frac{k_B T}{C2} [1 + \gamma (g_m + g_{mb}) R2] V_{rms}^2 \quad (4)$$

To verify the expression in (4), Kirchhoff's current law (KCL) at node  $d$  as earlier generated in (1) could be used with  $C_{gd}$  initially neglected. This is with the assumption that inherent capacitance  $C_{gd}$  is significantly smaller than the output capacitance  $C2$ .

$$\overline{i_{n,out2}^2} = \overline{i_{d,th}^2} + \overline{i_{d,1/f}^2} + \overline{i_{R2}^2} \quad (5)$$

$$\overline{v_{n,out2}^2} = \left[ 4k_B T \gamma (g_m + g_{mb}) \Delta f + \frac{K_f I_D}{L^2 C_{ox} f_{co}} \Delta f + \frac{4k_B T}{R2} \Delta f \right] \left( R2 \parallel \frac{1}{sC2} \right)^2 \quad (6)$$

At higher frequency, thermal noise of transistor dominates, hence flicker noise could be neglected.

$$\overline{v_{n,out2}^2} = \frac{k_B T}{C2} [1 + \gamma (g_m + g_{mb}) R2] V_{rms}^2 \quad (7)$$

Expression for the voltage noise of RFout2 in (7) confirms that of the computation in (4). This comes with the assumption that  $C_{gd}$  is negligible as compared to  $C2$ . Interestingly, the expression for output noise power is also the signal-to-noise ratio SNR at the output side. Increasing the resistance  $R2$  increases the output noise contribution. Furthermore, increasing the capacitance  $C2$  would decrease the output voltage noise but it would also decrease the circuit bandwidth or the cutoff frequency of RFout2. This design tradeoff is inevitable so one should consider the effectiveness of setting or limiting the output capacitance.

Using the expression for SNR given as the output noise voltage in (4,7), dynamic range of the circuit for the RFout2 side could be determined. Dynamic range is the ratio of the maximum signal power that the circuit can tolerate without distortion to noise level of circuit. Note that the largest signal that can be passed through the output of the circuit is limited by the supply voltage ( $V_{DD}$ ). Dynamic range is expressed as

$$DR_2 = 10 \log \frac{P_{signal}}{P_{noise2}} = 20 \log \frac{V_{max,rms}}{V_{noise2,rms}} = 20 \log \frac{\frac{1}{2} \cdot \frac{V_{DD}}{\sqrt{2}}}{\sqrt{\frac{k_B T}{C2} [1 + \gamma(g_m + g_{mb})R2]}} \quad (8)$$

$$DR_2 = 10 \log \frac{V_{DD}^2 \cdot C2}{k_B T [1 + \gamma(g_m + g_{mb})R2]} \text{ dB} \quad (9)$$

For RFout1, the output noise voltage contribution was determined starting with KCL at node s. Same assumption applies with inherent capacitance  $C_{gs}$  significantly smaller than the output capacitance  $C1$ .

$$\overline{i_{n,out1}^2} = \overline{i_{d,th}^2} + \overline{i_{d,1/f}^2} + \overline{i_{R1}^2} \quad (10)$$

$$\overline{v_{n,out1}^2} = \left[ 4k_B T \gamma(g_m + g_{mb}) \Delta f + \frac{K_f I_D}{L^2 C_{ox} f_{co}} \Delta f + \frac{4k_B T}{R1} \Delta f \right] \left( R1 \parallel \frac{1}{sC1} \right)^2 \quad (11)$$

With same previous assumptions applied, expression for output voltage noise of RFout1 could be derived.

$$\overline{v_{n,out1}^2} = 4k_B T \left[ \gamma(g_m + g_{mb}) + \frac{1}{R1} \right] \left( R1 \parallel \frac{1}{sC1} \right)^2 \Delta f \quad (12)$$

$$\overline{v_{n,out1}^2} = \frac{k_B T}{C1} [1 + \gamma(g_m + g_{mb})R1] V_{rms}^2 \quad (13)$$

Resembling that of the expression in (7), total output voltage noise of RFout1 depends on output loads  $R1$  and  $C1$ . With the same behavior as the other output, increasing the resistance  $R1$  increases the overall noise. Also, output capacitance  $C1$  has a large effect on the output noise performance. Dynamic range for the RFout1 output side is determined as

$$DR_1 = 10 \log \frac{P_{signal}}{P_{noise1}} = 20 \log \frac{V_{max,rms}}{V_{noise1,rms}} \quad (14)$$

$$DR_1 = 10 \log \frac{V_{DD}^2 \cdot C1}{k_B T [1 + \gamma(g_m + g_{mb})R1]} \text{ dB} \quad (15)$$

With loads for the two output nodes assumed to be equal, that is  $R1 = R2$  and  $C1 \approx C2$ , the two output noise voltages would be equal. Now, with the discussion of noise performance, total output noise power contribution,  $N_{m1,total}$  and  $N_{m2,total}$  (or simply  $N_{m1}$  and  $N_{m2}$ ), of the two outputs are given as

$$N_{m1,total} = G_{m1} N_i + N_{m,out1} = N_{m1} \quad (16)$$

$$N_{m2,total} = G_{m1} N_i + N_{m,out2} = N_{m2} \quad (17)$$

And the noise factors for the two outputs are derived as

$$F_{m1} = \frac{S_{im}}{N_{im}} \cdot \frac{N_{m,out1}}{S_{m,out1}} = \frac{N_{m1}}{G_{m1} N_i} = \frac{G_{m1} N_i + N_{m,out1}}{G_{m1} N_i} = 1 + \frac{N_{m,out1}}{G_{m1} N_i} \quad (18)$$

$$F_{m2} = \frac{S_{im}}{N_{im}} \cdot \frac{N_{m,out1}}{S_{m,out1}} = \frac{N_{m2}}{G_{m2} N_i} = \frac{G_{m2} N_i + N_{m,out2}}{G_{m2} N_i} = 1 + \frac{N_{m,out2}}{G_{m2} N_i} \quad (19)$$

Plugging in the input noise expression with input impedance ( $R_i$ ) not equal to the source resistance ( $R_s$ ), and the derived output noise contributions of RFout1 and RFout2 from (13) and (7), respectively,

$$F_{m1} = 1 + \frac{N_{m,out1}}{G_{m1} N_i} = 1 + \frac{\frac{k_B T}{C1} [1 + \gamma(g_m + g_{mb})R1]}{A_{v1} \cdot 4k_B T \frac{R_s R_i}{(R_s + R_i)^2} \Delta f} \quad (20)$$

$$F_{m2} = 1 + \frac{N_{m,out2}}{G_{m1} N_i} = 1 + \frac{\frac{k_B T}{C2} [1 + \gamma(g_m + g_{mb})R2]}{A_{v2} \cdot 4k_B T \frac{R_s R_i}{(R_s + R_i)^2} \Delta f} \quad (21)$$

$A_{v1}$  and  $A_{v2}$  are the voltage gains of the two outputs,  $v_{out1}$  and  $v_{out2}$ , respectively, with respect to the same input  $v_{in}$ . Simplifying (20) and (21), noise figures (NF) are then expressed as

$$NF_{m1} = 10\log(F_{m1}) = 10\log \left[ 1 + \frac{1 + \gamma(g_m + g_{mb})R1}{C1 \cdot 4 \frac{R_s R_i}{(R_s + R_i)^2} \Delta f \cdot A_{v1}} \right] \text{ dB} \quad (22)$$

$$NF_{m2} = 10\log(F_{m2}) = 10\log \left[ 1 + \frac{1 + \gamma(g_m + g_{mb})R2}{C2 \cdot 4 \frac{R_s R_i}{(R_s + R_i)^2} \Delta f \cdot A_{v2}} \right] \text{ dB} \quad (23)$$

If input impedance ( $R_i$ ) is matched with the source resistance ( $R_s$ ), noise factors would be expressed as

$$F_{m1} = 1 + \frac{1 + \gamma(g_m + g_{mb})R1}{C1 \cdot k_B T \Delta f \cdot A_{v1}} \quad (24)$$

$$F_{m2} = 1 + \frac{1 + \gamma(g_m + g_{mb})R2}{C2 \cdot k_B T \Delta f \cdot A_{v2}} \quad (25)$$

Noise figures are then computed as

$$NF_{m1} = 10\log \left[ 1 + \frac{1 + \gamma(g_m + g_{mb})R1}{C1 \cdot k_B T \Delta f \cdot A_{v1}} \right] \text{ dB} \quad (26)$$

$$NF_{m2} = 10\log \left[ 1 + \frac{1 + \gamma(g_m + g_{mb})R2}{C2 \cdot k_B T \Delta f \cdot A_{v2}} \right] \text{ dB} \quad (27)$$

Noise performance is an important design consideration since it determines the vulnerability of the active balun to unwanted signal like noise. Hence it is critically important that the active balun circuit contributes as little noise as possible in the system level design of radio frequency (RF) applications.

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